

**UPDATE OF THE AGEIT SOFTWARE TO INCORPORATE  
NATURAL AND FISHING MORTALITY IN THE ESTIMATION  
OF CATCH AT AGE FROM CATCH AT SIZE:  
APPLICATION TO THE AGEING OF YELLOWFIN TUNA CAS 2016**

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*SUMMARY*

*Age composition is important information to understand the dynamics of the fish populations. In the case of Atlantic tunas, due to the multinational, wide and varied distribution of fisheries, almost all sampling comes from commercial fisheries with few if any sampling for direct aging. Hence, most of the ageing for tunas is estimated from length frequency samples. In the case of tropical tunas the standard approach in ICCAT has been estimating catch at age (CAA) assuming a particular growth model and "slicing" the catch at size (CAS) at given fixed time intervals (quarterly). Recently, for both BET and YFT this approach was improved by incorporating variance of size at age in the growth model allowing estimating a probability of age at size for a given time interval.*

*RÉSUMÉ*

*La composition par âge constitue une information importante pour comprendre la dynamique des populations de poissons. Dans le cas des thonidés de l'Atlantique, en raison de la distribution multinationale, large et variée des pêcheries, pratiquement tout l'échantillonnage provient des pêcheries commerciales, avec un volume très limité, voire inexistant, d'échantillonnage aux fins de la détermination directe de l'âge. C'est pourquoi la plupart de la détermination de l'âge des thonidés est estimée à partir des échantillons de fréquence des longueurs. Dans le cas des thonidés tropicaux, l'approche standard de l'ICCAT a été d'estimer la prise par âge (CAA) en postulant un modèle de croissance particulier et en "découpant" la prise par taille (CAS) à des intervalles de temps fixes (trimestriellement). Récemment, pour le thon obèse et l'albacore, cette approche a été améliorée en incorporant la variance de la taille à l'âge dans le modèle de croissance, ce qui permet d'estimer une probabilité d'âge par taille pour un intervalle de temps donné.*

*RESUMEN*

*La composición por edad es una información importante para entender la dinámica de las poblaciones de peces. En el caso de túnidos del Atlántico, debido a la distribución amplia, multinacional y variada de las pesquerías, casi todo el muestreo procede de las pesquerías comerciales, con poco o nada de muestreo para determinación directa de la edad. Por tanto, la mayor parte de la edad de los túnidos se ha estimado a partir de muestras de frecuencias de tallas. En el caso de los túnidos tropicales, el enfoque estándar en ICCAT ha consistido en estimar la captura por edad (CAA) asumiendo un modelo de crecimiento específico y "recortando" la captura por talla (CAS) en intervalos de tiempo fijos determinados (trimestralmente). Recientemente, tanto para el patudo como para el rabil se ha mejorado este enfoque incorporando la variación de talla por edad en el modelo de crecimiento, lo que permite estimar una probabilidad de edad por talla para un intervalo de tiempo determinado.*

*KEYWORDS*

*Ageing, catch at age, catch at size, natural mortality*

## **Introduction**

Age composition is important information to understand the dynamics of the fish populations. Having annual length, weight and age information allows following year-classes through time to understand growth and specifics of the dynamics of fish stocks and its response to environmental and fishing mortalities. Size and age are often collected from fisheries and surveys; however appropriate sampling can be limited by resources or the

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characteristics of the fisheries. In the case of Atlantic tunas, due to the multinational, wide and varied distribution of fisheries, almost all sampling comes from commercial fisheries with few if any sampling for direct aging. Hence, most of the ageing for tunas is estimated from length frequency samples. There are two main approaches to “ageing” annual size data; length frequency analysis where the overall size distribution is de-convoluted into the size composition of each age class as a mixture of size distributions (MacDonald 1987), or assuming a particular growth model and estimating the probability of age at a given size, normally incorporating some variance of size at age (Schnute and Fournier 1980). There are also some alternative that combined both approaches, usually given some prior information for the mean size in the length frequency analysis (MacDonald and Pitcher 1979).

In the case of tropical tunas the standard approach in ICCAT has been estimating catch at age (CAA) assuming a particular growth model and “slicing” the catch at size (CAS) at given fixed time intervals (quarterly). For both BET and YFT in 2011 this approach was improved by incorporating variance of size at age in the growth model allowing estimating a probability of age at size for a time interval (Ortiz and Palma 2012). However, in this methodology it was assumed that for a given size all ages will have a probability only determined by the growth model ignoring that the number of fish of older ages is much lower due to the exponential decline in numbers at age as result of natural and other mortalities, e.g. the probability that a fish will survive until age  $x$  and reach size  $y$ .

## 1. Materials and Methods

In the algorithms for ageing CAS (R script Ageit) therefore, it was incorporated into the estimation of the probability of age at size the conditioning that numbers of fish at age are declining exponentially with increase in age due to natural and fishing mortality ( $Z = F + M$ ). In this case it was assumed the exponential decline of a single cohort through its time life. Specifically, the underlying survival curve  $\theta_a$  for age group  $a$  that is fully recruited to the sampling fishery.

$$\theta_a = c^{-Za}$$

Where  $c$  is a constant and  $Z$  is the total mortality. This assumption is satisfied when recruitment and mortality are constant over time for all age groups. This basically assumed an in equilibrium population, the algorithms input a vector of natural mortality at age ( $M_a$ ) constant for all years, and vector(s) of fishing mortality by age ( $F_a$ ) constant or variable by year. It is also assumed that the annual growth is constant and independent of density effects, the algorithm need to fix a given birthday time interval within the year.

The probability density function (pdf) of length  $f_a(L)$  for each age  $a$  is a function of the growth parameters user defined, assuming a Gaussian distribution with mean  $\mu_a$  and standard deviation  $\sigma_a$ , given by

$$f_a(L) = \frac{1}{\sqrt{2\pi} \sigma_a} \exp\left[-\frac{1}{2\sigma_a^2} (L - \mu_a)^2\right]$$

Then, the probability that a length measurement falls into interval  $l$  for age  $a$  is

$$\psi_{la} = \int_l^{l+1} f_a(L) dL$$

That is the area under the pdf that covers the interval length  $l$ . The expected number of individuals of age  $a$  is  $\theta_a$  while the expected number of individuals of age  $a$  and length  $l$  is  $\theta_a \psi_{la}$ . Finally the expected number of individuals of length  $l$  is then sum of probabilities over all ages,

$$L_l = L \sum_{a=r}^A \psi_{la} \theta_a$$

Thus, the probability of age at size  $p(\text{Age} | \text{size})$  is estimated as

$$\hat{p}(\text{Age} | \text{size}) = p(\text{Age} | \text{size} \theta_{L_{inf}, K, t_0, \sigma}) \times \frac{N_{age}}{\sum_{i=0}^{\max\_age} N_i}$$

Where  $N_{age}$  is the expected numbers of fish at age following the exponential decline of a cohort given the total mortality  $Z$ .

The algorithms were tested by using the same data input with the ageit program estimating probability of age at size considering or not a mortality-at-age vector.

As example, the CAS of yellowfin tuna was used to compare the estimated CAA results when included the expected exponential decline of the cohorts with age due to mortality. In this case it was only assumed a natural mortality component (e.g.  $F = 0$ ). It was assumed that yellowfin followed a von Bertalanffy growth model as defined by Draganik and Pelczarski (1984), with the following parameters: i) asymptotic size ( $L_{inf}$ ) = 192.24 cm. ii)  $K = 0.370$ . iii)  $t_0 = -0.0033$ , and iv) overall coefficient of variance of size at age = 0.1619 (**Figure 1**). The range of ages for analysis was set from age 0 to age 19 as the maximum age, and age 11 as the plus group. It was assumed that ages plus to maximum age have the same mortality and variance at size parameters. Probabilities of age at size were estimated for time period of 3 months (e.g. quarterly annual growth), with the birth of fish in the first quarter. The size interval was set to 1 cm FL.

The natural mortality by age vector ( $M_a$ ) (**Figure 2**) and the multiplier for the age coefficient of variance of size at age were:

	Age 0	Age 1	Age 2	Age 3	Age 4	Age 5	Age 6	Age 7	Age 8	Age 9	Age 10	Age 11+
Ma	1.758	0.889	0.672	0.576	0.525	0.495	0.476	0.463	0.455	0.450	0.446	0.443
CV m	0.9651	0.7003	0.4026	0.2677	0.2677	0.2677	0.2677	0.2677	0.2677	0.2677	0.2677	0.9651

## 2. Results and discussion

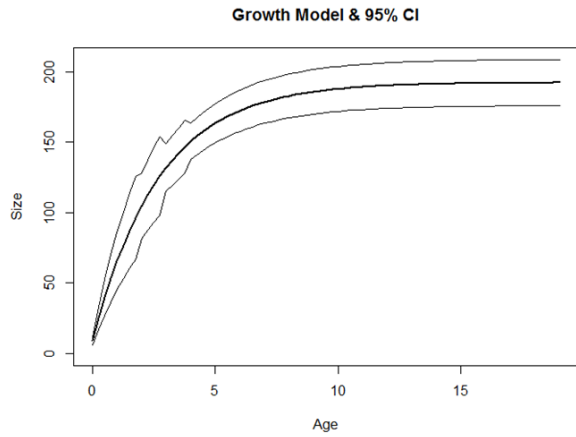
**Table 1** presents the estimated CAA matrices with and without considering mortality using the yellowfin 2016 CAS. As expected the number of fish per year are exactly the same, however the age distribution did varied. As expected when accounted for the decline in number of fish as they get older (**Figure 3**), the probability of age at size is shifted to younger age classes having higher probability at a given size (**Figure 4 and 5**).

In the case of yellowfin tuna catch at age is predominantly of younger ages 0 to 3 accounting for over 80% of the total catch (**Figure 6**). When taking into account the declines in number of fish due to mortality, at least natural mortality is clear that the catch proportions of younger ages increases markedly, particularly for age 1 through the whole time period, while the proportions of older ages decreased (**Figure 7**).

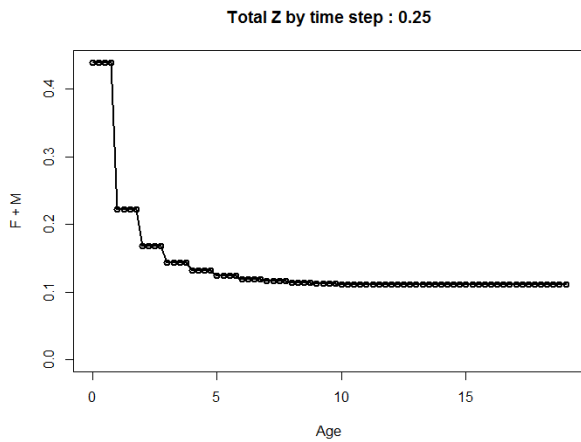
## References

- Cramer J. and M. Ortiz. 1999. Standardized catch rates for bigeye (*Thunnus obesus*) and yellowfin (*T. albacares*) from the U.S. longline fleet through 1997. Col. Vol. Sci. Pap. ICCAT 49(2):333-356.
- Draganik, B. and W. Pelczarski. 1984. Growth and age of bigeye and yellowfin tuna in the central Atlantic as per data gathered by RV WIECZNO. Col. Vol. Sci. Pap. ICCAT 20(1):96-103.
- Schnute, J.T. and D.A. Fournier. 1980. A new approach to length frequency analysis: growth structure. Can. J. Fish. Aquat. Sci. 37:1337-1351.
- MacDonald, P.D. 1987. Analysis of length frequency distributions. In Age and growth of fish. R.C. Summerfelt and G.E. Hall eds. Iowa State Univ. Press. Ames.
- MacDonald, P.D. and T.J. Pitcher. 1979. Age groups from size frequency data: a versatile and efficient method. J. Fish. Res. Board Can. 36:987-1001.
- Ortiz, M and C. Palma. 2012. Review of ageing protocols for Atlantic yellowfin tuna (*Thunnus albacares*). Col. Vol. Sci. Pap. ICCAT 68(3):984-994.

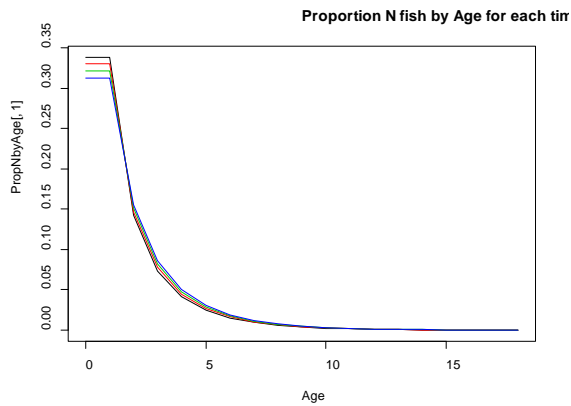




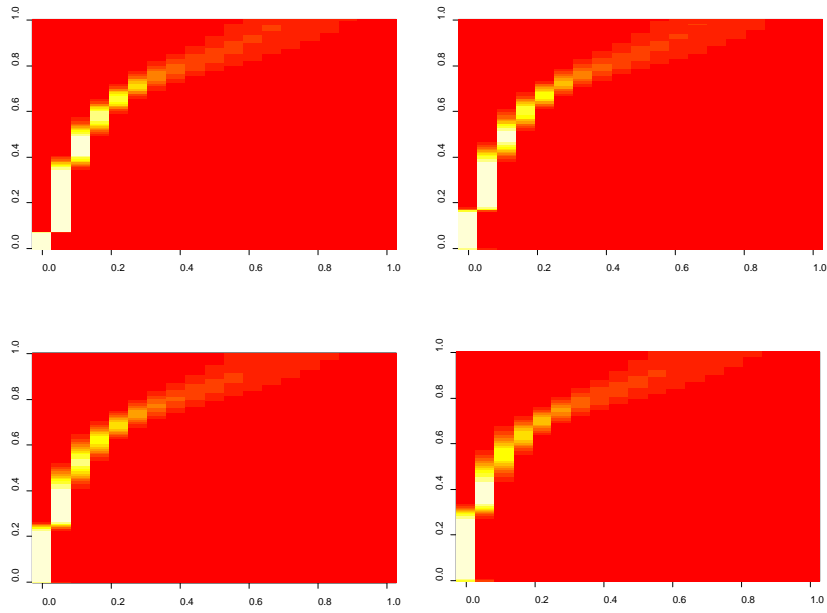
**Figure 1.** Assumed growth of size at age functional model (Draganik & Pel...) of yellowfin tuna with 95% confidence intervals to estimate CAA from size distribution of catch (CAS).



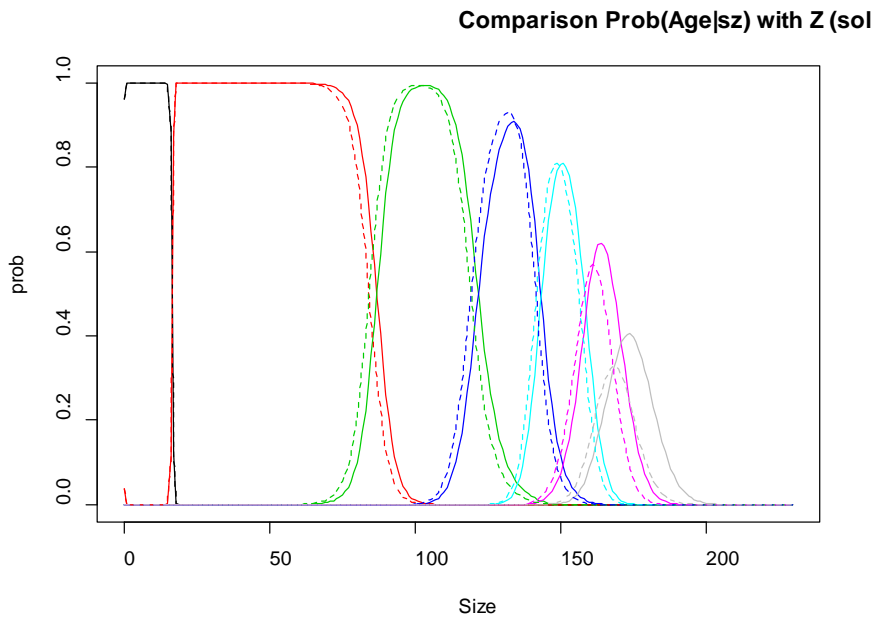
**Figure 2.** Assumed natural mortality at age and time step (quarter) for yellowfin tuna. ( $F = 0$ ).



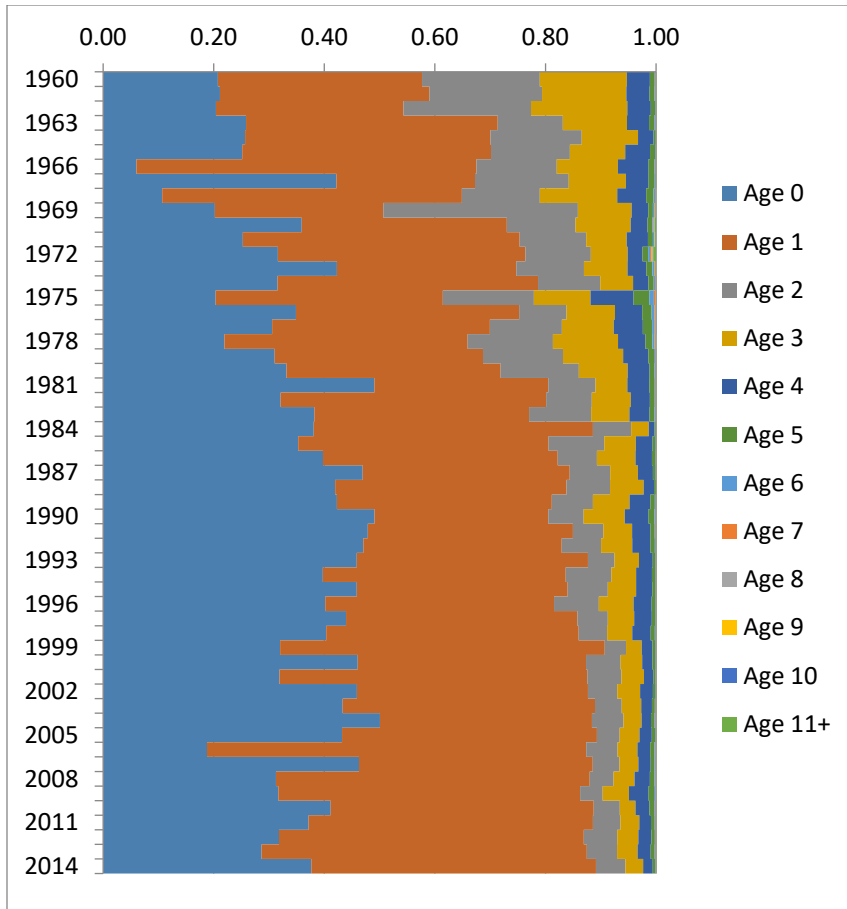
**Figure 3.** Estimated proportion of number of fish by age and quarter based on the exponential decline of cohorts due to mortality.



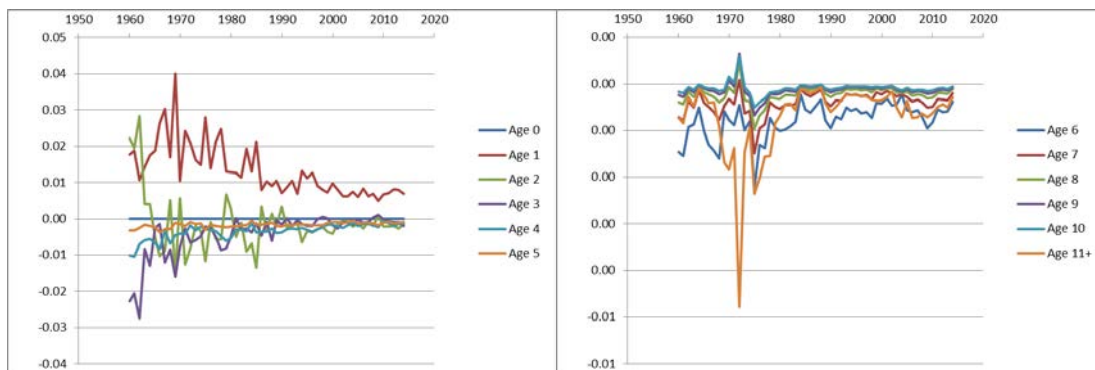
**Figure 4.** Level plot of the probability of size at age distribution for yellowfin tuna when mortality decline is considered. Each plot represents the quarterly probabilities with top-left being the quarter 1 (Jan-Mar) , top-right Q2 (Apr-Jun), bottom-left Q3 (Jul-Sep) and bottom-right Q4 (Oct-Dec). Higher probabilities indicated by white-yellow shades.



**Figure 5.** Comparison of the estimates probability of age at size ( $p(\text{Age}|\text{size})$ ) for yellowfin tuna when considering mortality of fish with age (solid lines) and when ignoring mortality (broken lines) for ages 0 to 6 (by colors).



**Figure 6.** Annual yellowfin tuna catch at age (CAA) distribution 1960 – 2014, as estimated with the ageit program assuming a von Bertalanffy growth model (Draganik and Pelzarski.) and natural mortality decline of cohorts.



**Figure 7.** Difference between the yellowfin age proportions by year and age from the CAA matrices estimated when considered it or not the decline in numbers of fish due to natural mortality. Positive values indicate that the respective proportion of CAA increases when considering natural mortality. Negative values indicate a lower proportion of those ages in the CAA when natural mortality was considered