

**UPDATE OF THE AGEIT SOFTWARE TO INCORPORATE  
NATURAL AND FISHING MORTALITY IN THE ESTIMATION  
OF CATCH AT AGE FROM CATCH AT SIZE:  
APPLICATION TO THE AGEING OF YELLOWFIN TUNA CAS 2016**

Mauricio Ortiz<sup>1</sup>

**SUMMARY**

*Age composition is important information to understand the dynamics of the fish populations. In the case of Atlantic tunas, due to the multinational, wide and varied distribution of fisheries, almost all sampling comes from commercial fisheries with few if any sampling for direct aging. Hence, most of the ageing for tunas is estimated from length frequency samples. In the case of tropical tunas the standard approach in ICCAT has been estimating catch at age (CAA) assuming a particular growth model and “slicing” the catch at size (CAS) at given fixed time intervals (quarterly). Recently, for both BET and YFT this approach was improved by incorporating variance of size at age in the growth model allowing estimating a probability of age at size for a given time interval.*

**RÉSUMÉ**

*La composition par âge constitue une information importante pour comprendre la dynamique des populations de poissons. Dans le cas des thonidés de l'Atlantique, en raison de la distribution multinationale, large et variée des pêcheries, pratiquement tout l'échantillonnage provient des pêcheries commerciales, avec un volume très limité, voire inexistant, d'échantillonnage aux fins de la détermination directe de l'âge. C'est pourquoi la plupart de la détermination de l'âge des thonidés est estimée à partir des échantillons de fréquence des longueurs. Dans le cas des thonidés tropicaux, l'approche standard de l'ICCAT a été d'estimer la prise par âge (CAA) en postulant un modèle de croissance particulier et en "découpant" la prise par taille (CAS) à des intervalles de temps fixes (trimestriellement). Récemment, pour le thon obèse et l'albacore, cette approche a été améliorée en incorporant la variance de la taille à l'âge dans le modèle de croissance, ce qui permet d'estimer une probabilité d'âge par taille pour un intervalle de temps donné.*

**RESUMEN**

*La composición por edad es una información importante para entender la dinámica de las poblaciones de peces. En el caso de túnidos del Atlántico, debido a la distribución amplia, multinacional y variada de las pesquerías, casi todo el muestreo procede de las pesquerías comerciales, con poco o nada de muestreo para determinación directa de la edad. Por tanto, la mayor parte de la edad de los túnidos se ha estimado a partir de muestras de frecuencias de tallas. En el caso de los túnidos tropicales, el enfoque estándar en ICCAT ha consistido en estimar la captura por edad (CAA) asumiendo un modelo de crecimiento específico y "recortando" la captura por talla (CAS) en intervalos de tiempo fijos determinados (trimestralmente). Recientemente, tanto para el patudo como para el rabil se ha mejorado este enfoque incorporando la variación de talla por edad en el modelo de crecimiento, lo que permite estimar una probabilidad de edad por talla para un intervalo de tiempo determinado.*

**KEYWORDS**

*Ageing, catch at age, catch at size, natural mortality*

**Introduction**

Age composition is important information to understand the dynamics of the fish populations. Having annual length, weight and age information allows following year-classes through time to understand growth and specifics of the dynamics of fish stocks and its response to environmental and fishing mortalities. Size and age are often collected from fisheries and surveys; however appropriate sampling can be limited by resources or the

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<sup>1</sup> ICCAT Secretariat C/ Corazón de María 8, 6<sup>th</sup> floor Madrid 28002, Madrid Spain.

characteristics of the fisheries. In the case of Atlantic tunas, due to the multinational, wide and varied distribution of fisheries, almost all sampling comes from commercial fisheries with few if any sampling for direct aging. Hence, most of the ageing for tunas is estimated from length frequency samples. There are two main approaches to “ageing” annual size data; length frequency analysis where the overall size distribution is de-convoluted into the size composition of each age class as a mixture of size distributions (MacDonald 1987), or assuming a particular growth model and estimating the probability of age at a given size, normally incorporating some variance of size at age (Schnute and Fournier 1980). There are also some alternative that combined both approaches, usually given some prior information for the mean size in the length frequency analysis (MacDonald and Pitcher 1979).

In the case of tropical tunas the standard approach in ICCAT has been estimating catch at age (CAA) assuming a particular growth model and “slicing” the catch at size (CAS) at given fixed time intervals (quarterly). For both BET and YFT in 2011 this approach was improved by incorporating variance of size at age in the growth model allowing estimating a probability of age at size for a time interval (Ortiz and Palma 2012). However, in this methodology it was assumed that for a given size all ages will have a probability only determined by the growth model ignoring that the number of fish of older ages is much lower due to the exponential decline in numbers at age as result of natural and other mortalities, e.g. the probability that a fish will survive until age  $x$  and reach size  $y$ .

## 1. Materials and Methods

In the algorithms for ageing CAS (R script Ageit) therefore, it was incorporated into the estimation of the probability of age at size the conditioning that numbers of fish at age are declining exponentially with increase in age due to natural and fishing mortality ( $Z = F + M$ ). In this case it was assumed the exponential decline of a single cohort through its time life. Specifically, the underlying survival curve  $\theta_a$  for age group  $a$  that is fully recruited to the sampling fishery.

$$\theta_a = c^{-za}$$

Where  $c$  is a constant and  $Z$  is the total mortality. This assumption is satisfied when recruitment and mortality are constant over time for all age groups. This basically assumed an in equilibrium population, the algorithms input a vector of natural mortality at age ( $M_a$ ) constant for all years, and vector(s) of fishing mortality by age ( $F_a$ ) constant or variable by year. It is also assumed that the annual growth is constant and independent of density effects, the algorithm need to fix a given birthday time interval within the year.

The probability density function (pdf) of length  $f_a(L)$  for each age  $a$  is a function of the growth parameters user defined, assuming a Gaussian distribution with mean  $\mu_a$  and standard deviation  $\sigma_a$ , given by

$$f_a(L) = \frac{1}{\sqrt{2\pi} \sigma_a} \exp \left[ \frac{1}{2\sigma_a^2} (L - \mu_a)^2 \right]$$

Then, the probability that a length measurement falls into interval  $l$  for age  $a$  is

$$\psi_{la} = \int_l^{l+1} f_a(L) dL$$

That is the area under the pdf that covers the interval length  $l$ . The expected number of individuals of age  $a$  is  $\theta_a$  while the expected number of individuals of age  $a$  and length  $l$  is  $\theta_a \psi_{la}$ . Finally the expected number of individuals of length  $l$  is then sum of probabilities over all ages,

$$L_l = L \sum_{a=r}^A \psi_{la} \theta_a$$

Thus, the probability of age at size  $p(Age | size)$  is estimated as

$$\hat{p}(Age | size) = p(Age | size \theta_{L_{inf}, K, to, \sigma}) \times \frac{N_{age}}{\sum_{i=0}^{\max\_age} N_i}$$

Where  $N_{age}$  is the expected numbers of fish at age following the exponential decline of a cohort given the total mortality Z.

The algorithms were tested by using the same data input with the ageit program estimating probability of age at size considering or not a mortality-at-age vector.

As example, the CAS of yellowfin tuna was used to compare the estimated CAA results when included the expected exponential decline of the cohorts with age due to mortality. In this case it was only assumed a natural mortality component (e.g. F = 0). It was assumed that yellowfin followed a von Bertalanffy growth model as defined by Draganik and Pelczarski (1984), with the following parameters: i) asymptotic size ( $L_{inf}$ ) = 192.24 cm. ii)  $K = 0.370$ . iii)  $t_0 = -0.0033$ , and iv) overall coefficient of variance of size at age = 0.1619 (**Figure 1**). The range of ages for analysis was set from age 0 to age 19 as the maximum age, and age 11 as the plus group. It was assumed that ages plus to maximum age have the same mortality and variance at size parameters. Probabilities of age at size were estimated for time period of 3 months (e.g. quarterly annual growth), with the birth of fish in the first quarter. The size interval was set to 1 cm FL.

The natural mortality by age vector ( $M_a$ ) (**Figure 2**) and the multiplier for the age coefficient of variance of size at age were:

	Age 0	Age 1	Age 2	Age 3	Age 4	Age 5	Age 6	Age 7	Age 8	Age 9	Age 10	Age 11+
Ma	1.758	0.889	0.672	0.576	0.525	0.495	0.476	0.463	0.455	0.450	0.446	0.443
CV m	0.9651	0.7003	0.4026	0.2677	0.2677	0.2677	0.2677	0.2677	0.2677	0.2677	0.2677	0.9651

## 2. Results and discussion

**Table 1** presents the estimated CAA matrices with and without considering mortality using the yellowfin 2016 CAS. As expected the number of fish per year are exactly the same, however the age distribution did varied. As expected when accounted for the decline in number of fish as they get older (**Figure 3**), the probability of age at size is shifted to younger age classes having higher probability at a given size (**Figure 4 and 5**).

In the case of yellowfin tuna catch at age is predominantly of younger ages 0 to 3 accounting for over 80% of the total catch (**Figure 6**). When taking into account the declines in number of fish due to mortality, at least natural mortality is clear that the catch proportions of younger ages increases markedly, particularly for age 1 through the whole time period, while the proportions of older ages decreased (**Figure 7**).

## References

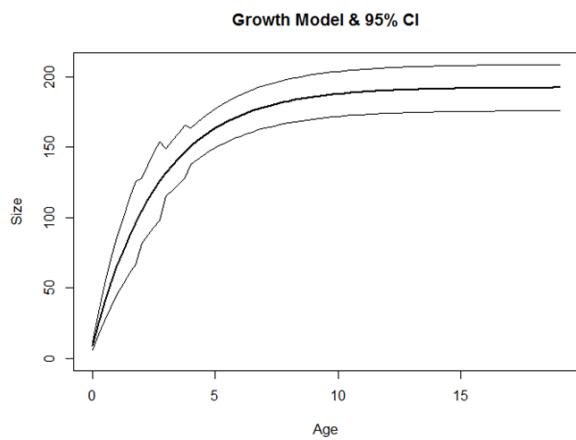
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**Table 1.** Estimated yellowfin tuna CAA matrices with and without considering age mortality decline of cohorts.

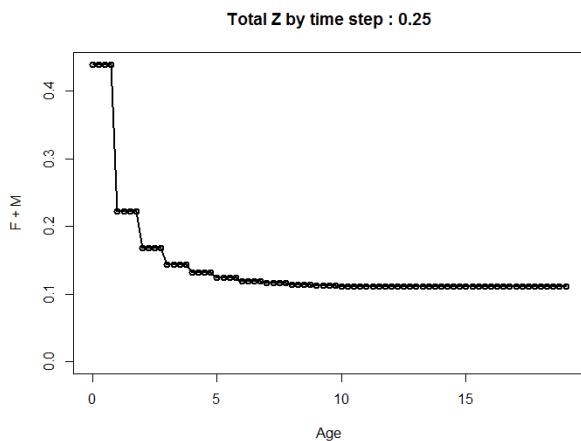
Estimation with out Mortality at age consideration

YearC	Age 0	Age 1	Age 2	Age 3	Age 4	Age 5	Age 6	Age 7	Age 8	Age 9	Age 10	Age 11+	Total
1960	533,673	904,895	490,781	463,470	133,399	30,215	8,545	3,046	1,372	760	495	1,942	2,572,595
1961	467,368	796,425	407,511	383,024	115,804	26,910	7,878	2,883	1,319	737	483	1,909	2,212,251
1962	474,281	763,713	470,197	468,503	115,525	23,511	5,382	1,569	609	305	187	676	2,324,457
1963	870,375	1,484,822	383,591	418,148	154,826	36,651	10,949	3,779	1,574	803	489	1,691	3,367,699
1964	975,897	1,622,609	612,215	436,987	127,899	22,118	3,856	930	328	160	99	393	3,803,490
1965	907,345	1,554,823	533,495	370,928	185,800	40,295	9,473	2,615	953	457	272	961	3,607,416
1966	1,645,965	434,676	313,503	178,048	40,858	9,299	2,708	1,060	538	334	1,248	2,796,463	
1967	1,197,481	626,145	506,272	327,429	126,875	38,993	9,773	2,854	1,088	535	324	1,224	2,838,994
1968	394,042	1,938,672	502,092	547,920	217,880	59,905	17,155	5,689	2,424	1,313	870	4,357	3,692,319
1969	811,014	1,061,583	1,473,681	454,303	137,675	38,237	13,673	5,909	3,093	1,970	1,497	10,110	4,012,750
1970	1,585,590	1,592,318	522,898	475,381	152,704	44,175	13,701	5,128	2,574	1,753	1,553	18,115	4,415,891
1971	1,089,165	2,051,853	573,599	327,325	182,715	48,162	14,169	5,266	2,522	1,571	1,251	11,851	4,309,448
1972	1,756,804	2,371,700	702,225	406,275	160,890	60,488	22,185	9,598	5,721	4,709	4,732	52,505	5,557,833
1973	2,446,888	1,782,133	720,218	490,947	214,974	72,606	25,394	9,838	4,603	2,697	1,970	14,683	5,786,950
1974	2,475,012	3,579,613	910,236	503,299	236,973	82,754	29,000	11,480	5,398	3,037	1,994	7,873	7,846,668
1975	1,064,324	2,003,135	923,552	546,341	422,324	164,728	55,155	20,600	9,353	5,170	3,365	13,188	5,231,235
1976	2,516,582	2,814,718	624,586	651,646	375,956	136,076	47,394	18,838	9,153	5,371	3,662	15,533	7,219,513
1977	2,037,743	2,481,837	905,667	660,039	373,091	125,705	41,215	15,601	7,265	4,120	2,739	11,160	6,666,183
1978	1,436,876	2,720,549	1,048,119	829,898	356,089	96,932	28,986	11,344	5,654	3,455	2,487	13,184	6,553,574
1979	2,124,056	2,490,400	945,541	799,506	355,502	85,804	23,657	8,532	3,946	2,247	1,504	6,229	6,846,924
1980	2,629,928	2,964,673	1,101,341	738,831	357,764	87,459	24,607	8,849	4,021	2,237	1,463	5,751	7,926,924
1981	6,123,137	3,772,565	1,128,586	717,804	537,076	145,794	36,483	11,378	4,643	2,409	1,509	5,645	12,487,029
1982	4,058,805	5,935,250	1,055,636	934,399	473,193	133,070	35,747	11,559	4,763	2,460	1,526	5,542	12,651,950
1983	4,483,135	4,329,738	1,423,007	843,198	467,424	123,930	34,437	11,913	5,233	2,845	1,833	7,070	11,733,763
1984	4,656,686	6,017,650	926,753	438,929	140,494	34,030	8,735	2,862	1,204	634	396	1,460	12,229,831
1985	4,388,118	5,365,717	1,419,794	725,066	424,655	85,934	17,840	4,959	1,871	916	549	1,901	12,437,319
1986	4,783,158	5,009,093	815,541	893,215	402,257	91,214	20,644	6,079	2,375	1,187	721	2,536	12,028,022
1987	6,508,710	5,048,048	1,059,671	706,387	428,750	83,147	17,723	5,114	1,986	994	605	2,152	13,863,287
1988	5,431,074	5,295,891	1,001,214	861,180	279,863	54,643	10,696	2,812	1,019	484	284	950	12,940,111
1989	5,653,588	5,058,181	1,017,582	893,525	557,195	133,851	32,532	10,425	4,421	2,369	1,519	5,876	13,371,063
1990	7,302,394	4,570,109	903,354	1,131,702	697,853	185,932	48,119	15,863	6,832	3,701	2,393	3,989	14,877,642
1991	7,413,844	5,608,871	884,416	802,690	561,987	145,325	37,443	12,573	5,555	3,075	2,020	8,107	15,485,905
1992	6,790,992	5,026,611	1,055,544	841,711	515,213	139,202	35,409	11,335	4,669	2,410	1,493	5,403	14,429,993
1993	8,352,319	7,483,710	892,483	814,030	505,427	114,444	25,301	7,672	3,172	1,688	1,089	4,439	18,205,774
1994	6,342,360	6,800,115	1,417,894	739,592	496,109	120,401	26,786	8,001	3,254	1,702	1,076	4,099	15,961,388
1995	6,555,866	5,291,747	1,083,661	763,389	458,104	101,941	22,501	6,847	2,838	1,502	956	3,659	14,293,011
1996	4,883,768	4,873,679	1,032,828	786,874	404,878	100,117	22,509	6,760	2,728	1,406	876	3,232	12,155,655
1997	5,890,048	5,492,228	777,287	642,110	464,054	106,643	23,321	7,034	2,915	1,553	997	3,911	13,412,101
1998	5,670,916	6,308,181	757,454	629,883	499,922	134,667	32,519	10,061	4,104	2,126	1,327	4,911	14,056,071
1999	5,705,633	10,339,608	745,572	503,669	377,902	102,890	26,875	9,055	4,071	2,345	1,621	7,454	17,826,451
2000	6,994,678	6,126,948	1,011,276	619,676	304,704	87,312	25,077	8,847	3,969	2,205	1,450	5,851	15,191,994
2001	5,652,038	9,723,800	1,111,036	772,482	336,580	79,962	21,283	7,484	3,415	1,928	1,280	5,212	17,716,499
2002	7,064,288	6,339,010	820,297	653,737	391,644	90,238	20,518	6,166	2,464	1,253	769	2,746	15,393,130
2003	6,367,631	6,619,744	719,315	535,682	313,750	90,734	27,292	10,317	4,900	2,828	1,903	7,863	14,701,958
2004	7,538,683	5,668,017	889,442	519,361	277,958	94,393	34,052	14,518	7,316	4,310	2,906	11,784	15,062,739
2005	5,383,685	5,672,430	527,744	450,338	300,429	86,600	23,971	8,137	3,536	1,916	1,236	4,810	12,464,831
2006	2,130,881	7,683,835	670,684	420,849	277,958	95,186	30,739	11,735	5,553	3,197	2,151	8,934	11,341,703
2007	5,296,046	4,765,787	561,637	400,247	270,038	90,297	28,494	10,830	5,172	3,023	2,066	8,915	11,442,552
2008	3,694,886	6,624,867	530,795	445,119	349,078	111,810	32,978	11,758	5,318	2,983	1,980	8,171	11,819,744
2009	3,508,099	5,987,469	438,917	514,681	418,990	130,992	37,713	13,248	5,921	3,274	2,140	8,482	11,069,925
2010	5,309,076	6,051,928	637,527	370,756	330,188	128,565	40,644	14,547	6,419	3,477	2,229	8,519	12,903,874
2011	4,562,592	6,229,764	636,673	427,506	277,149	93,011	28,273	10,102	4,519	2,490	1,621	6,387	12,280,086
2012	3,689,638	6,303,556	725,074	454,769	296,397	86,551	25,025	8,776	3,868	2,114	1,377	5,577	11,602,721
2013	3,040,359	6,157,913	607,421	401,070	269,546	85,548	25,726	9,198	4,100	2,247	1,456	5,681	10,610,265
2014	4,700,562	6,346,227	680,032	427,219	234,914	65,722	17,958	6,118	2,675	1,459	946	3,737	12,487,571

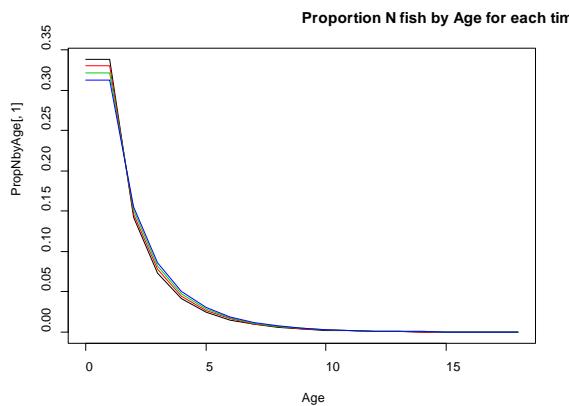
YearC	Age 0	Age 1	Age 2	Age 3	Age 4	Age 5	Age 6	Age 7	Age 8	Age 9	Age 10	Age 11+	Total
1960	533,752	950,170	547,719	404,954	107,537	21,863	4,793	1,197	362	132	56	60	2,572,595
1961	467,438	838,038	450,790	337,400	92,817	19,561	4,466	1,145	352	129	55	59	2,212,251
1962	474,349	788,374	536,009	404,564	99,221	17,630	3,233	721	210	77	33	36	2,324,457
1963	870,506	1,533,099	396,700	390,405	134,623	31,253	8,036	2,081	611	213	87	86	3,367,699
1964	976,038	1,688,913	627,276	387,618	106,652	14,447	1,923	377	121	54	29	42	3,803,490
1965	907,477	1,622,642	514,567	361,790	161,775	31,694	5,775	1,165	313	111	48	53	3,607,416
1966	1,68,243	1,719,633	406,087	309,548	154,844	30,347	5,673	1,327	416	166	79	100	2,796,463
1967	1,197,550	711,987	481,159	293,120	116,933	30,802	5,696	1,153	304	110	56	124	2,838,994
1968													



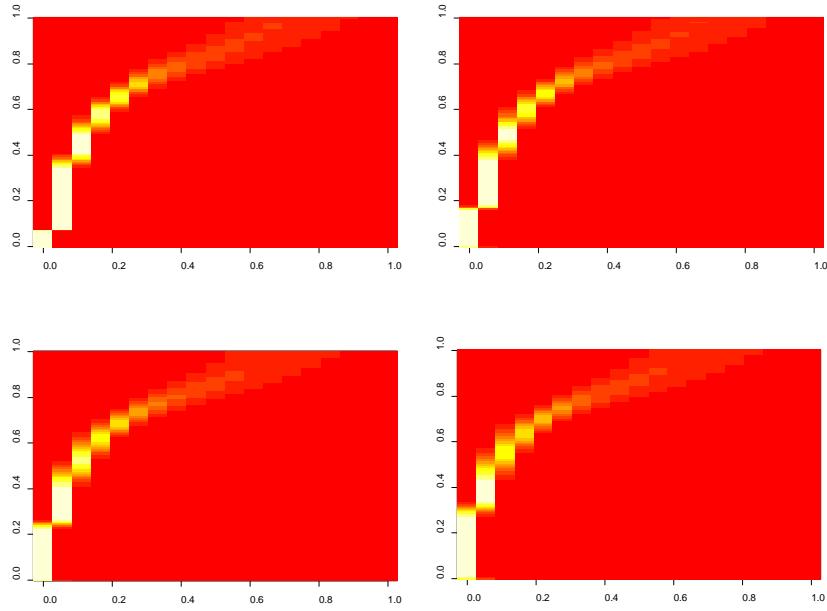
**Figure 1.** Assumed growth of size at age functional model (Draganik & Pel...) of yellowfin tuna with 95% confidence intervals to estimate CAA from size distribution of catch (CAS).



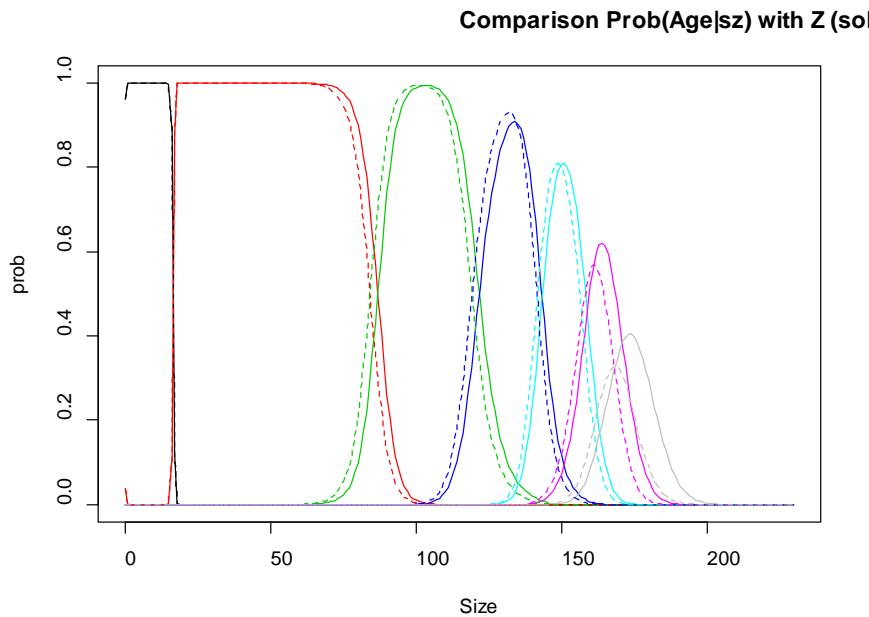
**Figure 2.** Assumed natural mortality at age and time step (quarter) for yellowfin tuna. ( $F = 0$ ).



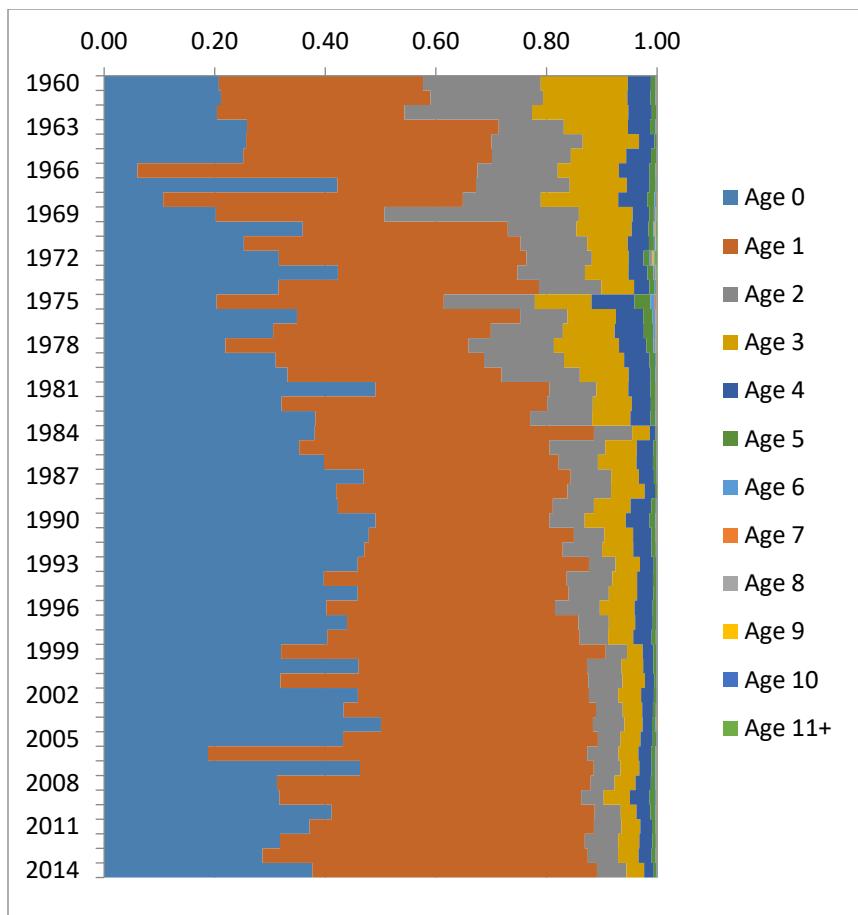
**Figure 3.** Estimated proportion of number of fish by age and quarter based on the exponential decline of cohorts due to mortality.



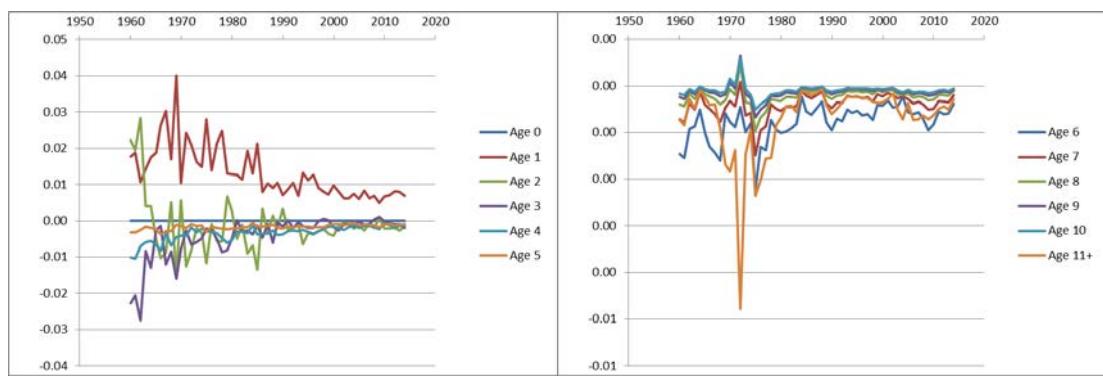
**Figure 4.** Level plot of the probability of size at age distribution for yellowfin tuna when mortality decline is considered. Each plot represents the quarterly probabilities with top-left being the quarter 1 (Jan-Mar) , top-right Q2 (Apr-Jun), bottom-left Q3 (Jul-Sep) and bottom-right Q4 (Oct-Dec). Higher probabilities indicated by white-yellow shades.



**Figure 5.** Comparison of the estimates probability of age at size ( $p(\text{Age}|\text{size})$ ) for yellowfin tuna when considering mortality of fish with age (solid lines) and when ignoring mortality (broken lines) for ages 0 to 6 (by colors).



**Figure 6.** Annual yellowfin tuna catch at age (CAA) distribution 1960 – 2014, as estimated with the ageit program assuming a von Bertalanffy growth model (Draganik and Pelzarski.) and natural mortality decline of cohorts.



**Figure 7.** Difference between the yellowfin age proportions by year and age from the CAA matrices estimated when considered it or not the decline in numbers of fish due to natural mortality. Positive values indicate that the respective proportion of CAA increases when considering natural mortality. Negative values indicate a lower proportion of those ages in the CAA when natural mortality was considered